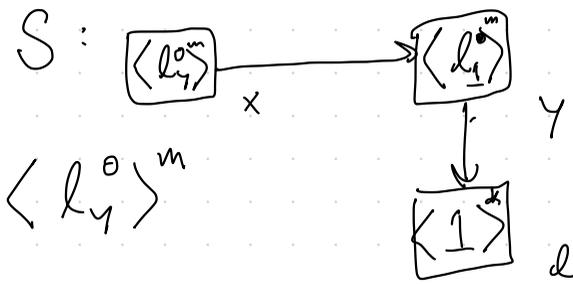


FR Semantics (II)

- ▶ Location: abstract entity w/ id. l_x named l_5 unnamed
- ▶ Values: unit (ϵ), integer (i32), reference l_i^0 borrowed l_i^1 owned
- ▶ Partial Value: value or none (\perp)
- ▶ Slot Value: Par. Val. + lifetime, $\langle v \rangle^m$
- ▶ Store: map from loc. to slot value

$$\{ l_x \mapsto \langle l_y^0 \rangle^m, l_y \mapsto \langle l_1^0 \rangle^m, l_1 \mapsto \langle \perp \rangle^* \}$$



$$S(l_x) = \langle l_y^0 \rangle^m$$

$$loc(S, **x) = l_1$$

```

let mut y = box 1;
let mut x = &y;
  
```

global lifetime

Store Interface :

$\text{loc}(S, w)$: locate lval
└─┬─
lval

$\text{read}(S, w)$:

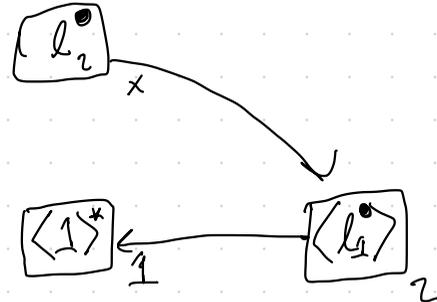
$\text{write}(S, w, v)$
└─┬─┬─
lval partial

$\text{drop}(S, \ell)$
└─┬─
list of partial value

list of partial value

Drop :

ex. $\text{let mut } x = \text{Box}::\text{new}(\text{Box}::\text{new}(1))$



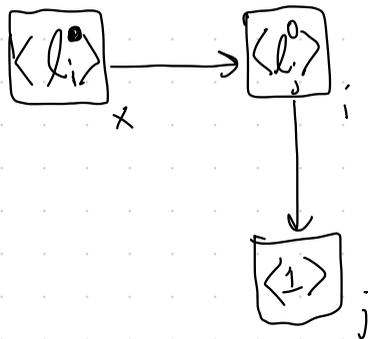
Def:

$$(i) \text{ drop}(S, \emptyset) = S$$

$$(ii) \text{ drop}(S, \psi \cup \{v^\perp\}) = \text{drop}(S, \psi) \text{ if } v^\perp \neq l_x^\bullet$$

$$(iii) \text{ drop}(S, \psi \cup \{l_x^\bullet\}) =$$

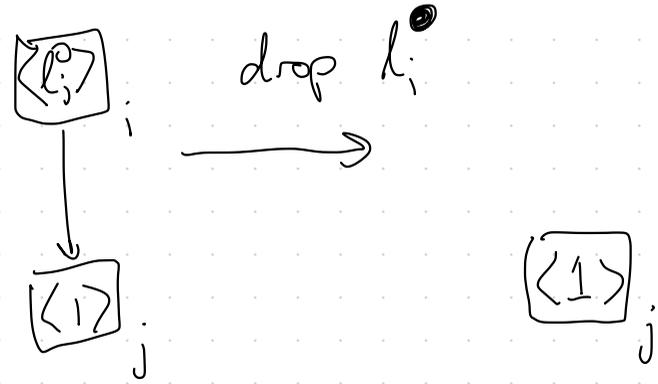
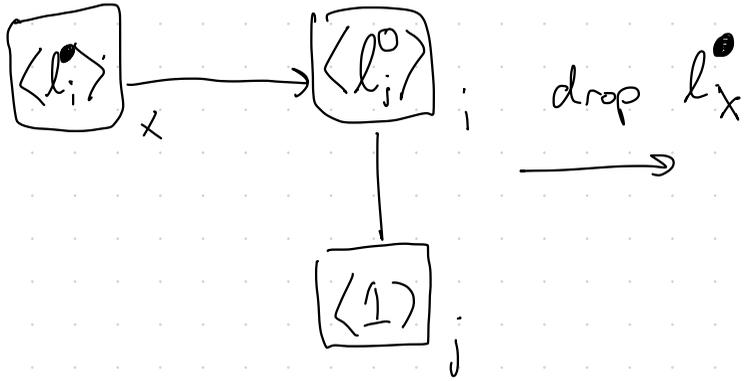
$$\text{drop}(S \setminus \{l \mapsto \langle v^\perp \rangle\}, \psi \cup \{v^\perp\}) \text{ where}$$



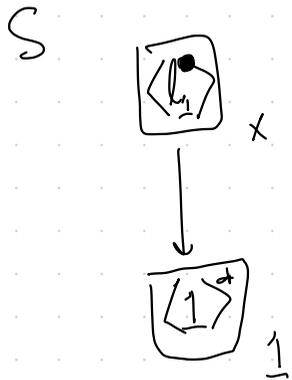
$$\begin{aligned} \text{drop}(S, \{l_x^\bullet\}) &= \text{drop}(S \setminus \{l_x \mapsto \langle l_i^\bullet \rangle\}, \{l_i^\bullet\}) \\ &\xrightarrow{\quad} = \text{drop}(S' \setminus \{l_i \mapsto \langle l_i^0 \rangle\}, \{l_i^0\}) \\ &= S' \setminus \{l_i \mapsto l_i^0\} \end{aligned}$$

$S(l) = \langle v^\perp \rangle$

omitted



let mut x = Box::new(1);



$\text{drop}(S, \{ l_x^0 \}) =$

$\text{drop}(S \setminus \{ l_x \mapsto \langle l_1^0 \rangle \}, \{ l_1 \})$

$S \setminus \{ l_x \mapsto \langle l_1^0 \rangle, l_1 \mapsto \langle 1 \rangle^* \}$

$$S_2 = \text{drop}(S_1, \{v\})$$

$$\frac{\langle S_1 \triangleright v; \vec{t} \rightarrow S_2 \triangleright \vec{t} \rangle^l}{(R\text{-SEQ})}$$

$$\langle S_1 \triangleright t_1 \rightarrow S_2 \triangleright t_2 \rangle^l$$

$$\frac{\langle S_1 \triangleright t_1; \vec{t} \rightarrow S_2 \triangleright t_2; \vec{t} \rangle^l}{(R\text{-SUB})}$$

$$\langle S_1 \triangleright \vec{t}_1 \rightarrow S_2 \triangleright \vec{t}_2 \rangle^m$$

$$\frac{\langle S_1 \triangleright \{\vec{t}_1\}^m \rightarrow S_2 \triangleright \{\vec{t}_2\}^m \rangle^l}{(R\text{-BLOCK A})}$$

$\text{drop}(S_1, m) \longleftarrow \text{drop}(S_1, \{v : \exists l, S(l) = \langle v \rangle^m\})$

$\langle S_1 \triangleright \{v\}^m \longrightarrow S_2 \triangleright v \rangle$

Example

let mut x = 1;
let mut y = box x;

let mut z = box 0;

y = z;

* y

} m;

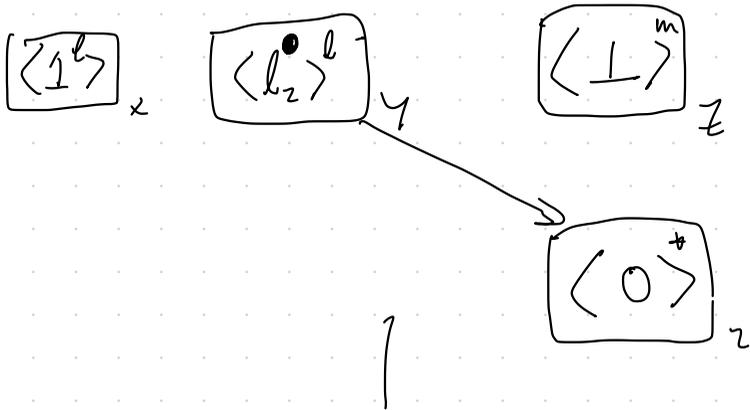
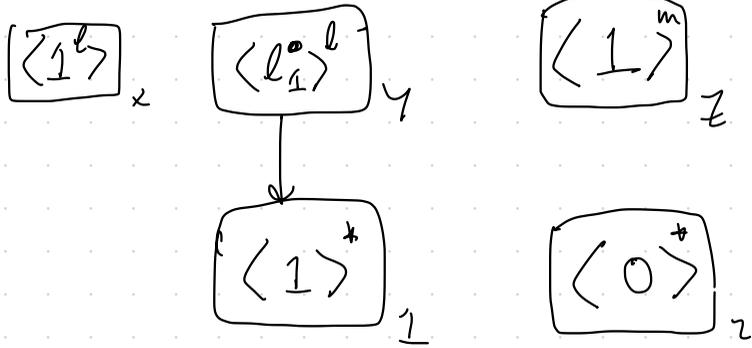
S: $\emptyset \rightarrow \text{let mut } x = 1;$

S: $\langle 1 \rangle^l_x \rightarrow \text{let mut } y = \text{box } 1;$

S: $\langle 1 \rangle^l_x \quad \langle l_1 \rangle^l_y \rightarrow \text{let mut } z = \text{box } 0;$
 \downarrow
 $\langle 1 \rangle^*_1$

S: $\langle 1 \rangle^l_x \quad \langle l_1 \rangle^l_y \quad \langle l_2 \rangle^m_z$
 $\downarrow \quad \downarrow$
 $\langle 1 \rangle^*_1 \quad \langle 0 \rangle^*_z$

$$y = z \longrightarrow y = l_2^{\textcircled{2}}$$



$$\longrightarrow \text{let } y = l_2^{\textcircled{2}} ;$$

$\rightarrow \dagger y \rightarrow 0$

